

1. (1 point) Solve  $|x + 4| + 3 < 5$ . Write your answer in interval notation.

$$\begin{aligned} |x+4| &< 2 & -6 < x < -2 \\ -2 < x+4 < 2 & \end{aligned}$$
$$\boxed{(-6, -2)}$$

2. (2.5 points) Find the center and radius of the circle given by the equation  $2x^2 + 2y^2 - 12x + 8y - 24 = 0$ .

$$\begin{aligned} 2x^2 + 2y^2 - 12x + 8y - 24 &= 0 \\ x^2 + y^2 - 6x + 4y &= 12 \\ (x^2 - 6x + 9) + (y^2 + 4y + 4) &= 12 + 9 + 4 \\ (x-3)^2 + (y+2)^2 &= 25 \end{aligned}$$
$$\boxed{\begin{array}{l} \text{center: } (3, -2) \\ \text{radius: } 5 \end{array}}$$

3. Let  $P_1 = (-2, 3)$  and  $P_2 = (2, 1)$ .

- (a) (0.5 points) Find the distance between  $P_1$  and  $P_2$ .

$$\begin{aligned} d &= \sqrt{(2+2)^2 + (1-3)^2} \\ &= \sqrt{16+4} \end{aligned}$$

$$\boxed{d = 2\sqrt{5}}$$

- (b) (0.5 points) Find the midpoint between  $P_1$  and  $P_2$ .

$$M = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) = \boxed{(0, 2)}$$

- (c) (0.5 points) Find the equation of the line containing  $P_1$  and  $P_2$ .

$$m = \frac{1-3}{2+2} = \frac{-2}{4} = -\frac{1}{2}$$

$$y - 1 = -\frac{1}{2}(x - 2)$$

$$y - 1 = -\frac{1}{2}x + 1$$

$$\boxed{y = -\frac{1}{2}x + 2}$$